

2 (a) Solve the equation $\log_3(x-2) = \log_3(12-x) - 2$. [4]

(b) Given that $(2\log_5 y)(\log_x 5) = 8$, express y in terms of x . [3]

2 (a) Solve the equation $\log_3(x-2) = \log_3(12-x) - 2$.

[4]

$$\log_3(x-2) = \log_3(12-x) - 2 \quad \rightarrow \quad 2 \log_3 3$$

$$\log_3(x-2) = \log_3(12-x) - \log_3 3^2$$

$$\log_3(x-2) = \log_3\left(\frac{12-x}{9}\right) \quad \rightarrow \quad \text{compare}$$

$$x-2 = \frac{12-x}{9}$$

$$9(x-2) = 12-x$$

$$10x = 30$$

$$x = 3 \quad // \quad \text{Ans}$$

(b) Given that $(2 \log_5 y)(\log_x 5) = 8$, express y in terms of x .

[3]

$$\left(\frac{2 \log_x y}{\log_x 5}\right) (\log_x 5) = 8 \quad \rightarrow \quad \text{change of base formula}$$

$$\log_x y = 4$$

$$y = x^4$$